

The Forensic Statistical Tool, FST, is a statistical tool for analysis of complex forensic DNA mixtures and reference profiles, such as those from suspects or victims. The method employs a likelihood ratio, which is a standard analytical procedure, used in virtually every scientific field, including forensics. In addition, FST models allelic drop-out and drop-in. This means that FST can assign a weight to a comparison between an evidence profile and a reference profile when one or more of the reference profile's alleles are not detected in the mixture and/or when additional alleles are detected. Without this tool, it is not possible to assign a quantitative weight to such a comparison.

As a matter of background, in a conventional forensic LR framework, the probability of a crime scene DNA profile ( $G$ ) is computed under two competing hypotheses: that of the prosecution ( $H_p$ ) and that of the defense ( $H_d$ ). The LR is the ratio of these two probabilities:  $LR = \frac{\Pr(G | H_p)}{\Pr(G | H_d)}$ . In a typical simple scenario, the prosecution asserts that the crime scene DNA belongs to the suspect ( $H_p:S$ ) and the defense asserts that the crime scene DNA belongs to an unknown, unrelated individual ( $H_d:U$ ). If the crime scene profile matches the suspect profile, then  $\Pr(G | H_p) = 1.0$  and  $\Pr(G | H_d) = P$ , where  $P$  is the estimated population frequency of the crime scene profile (i.e., the random match probability, RMP). Thus, in this scenario,  $LR = \frac{1}{RMP}$  when the evidence profile matches the suspect profile. When a crime scene profile reflects a mixture, the conventional LR can also be used by specifying the appropriate  $H_p$  and  $H_d$ . For example, the prosecution may assert that the mixture includes the victim and

suspect ( $H_p:V+S$ ), while the defense may assert the mixture includes the victim and an unknown, unrelated individual ( $H_d:V+U$ ).

Multiple replicate amplifications of an evidentiary sample can be considered within a LR framework. Let  $\mathbf{R} = R_1, R_2, \dots, R_n$  represent the alleles observed in amplification replicates 1 through  $n$  at a single locus in an evidentiary sample. At NYC OCME, normally,  $n = 3$  for low template samples and  $n = 1$  or  $2$  for high template

samples. The replicate data are used to compute  $LR = \frac{\Pr(\mathbf{R} | H_p)}{\Pr(\mathbf{R} | H_d)}$ .

We have incorporated allelic drop-out and drop-in into the LR. A critical step in this process is to consider all possible genotypes for the unknown contributor(s) in the denominator (as well as the numerator for more complex scenarios). If  $x$  distinct alleles are observed at a locus in the evidentiary profile, there are  $m = \frac{x(x+1)}{2} + x + 1$  values comprising the set of possible genotypes of an unknown contributor. This calculation treats all unobserved alleles as a single 'other' allele. That is, an unknown contributor's genotype at the locus could include any pair wise combination of the observed alleles and the unobserved 'other' allele.

If  $H_p: S$  and  $H_d: U$ ,  $LR = \frac{\Pr(\mathbf{R} | S)}{\sum_{j=1}^m \Pr(\mathbf{R} | U = G_j) \Pr(U = G_j)}$ , where  $S$  represents the

suspect's alleles,  $U$  represents the alleles of an unknown contributor, and  $G_j$  represents the  $j^{\text{th}}$  possibility for the genotype of the unknown contributor.  $\Pr(U = G_j)$  is the expected population frequency of  $G_j$ , including a  $\theta$  correction for population substructure, applied to homozygous genotypes only, as recommended in the second

National Research Council Report (National Research Council. 1996. *The Evaluation of Forensic DNA Evidence*. National Academy Press, Washington DC). Note that this correction does not account for genotype correlation between individuals.

$$\text{If } H_p: S + V \text{ and } H_d: V + U, \quad LR = \frac{\Pr(\mathbf{R} | S, V)}{\sum_{j=1}^m \Pr(\mathbf{R} | V; U = G_j) \Pr(U = G_j)}$$

If  $H_p: S + U_1$  and  $H_d: U_2 + U_3$ ,

$$LR = \frac{\sum_{i=1}^m \Pr(\mathbf{R} | S; U_1 = G_i) \Pr(U_1 = G_i)}{\sum_{i=1}^m \sum_{j=1}^m \Pr(\mathbf{R} | U_2 = G_i, U_3 = G_j) \Pr(U_2 = G_i) \Pr(U_3 = G_j)}$$

All of the pairs of prosecutor and defense hypotheses shown in Table 1A are formulated similarly. Drop-out and drop-in rates are incorporated into  $\Pr(R_1, R_2, \dots, R_n | S)$  and  $\Pr(R_1, R_2, \dots, R_n | U = G_j)$ . Separate parameters are used for partial drop-out of heterozygotes, complete drop-out of heterozygotes, and complete drop-out of homozygotes. Drop-out rates were estimated empirically as a function of locus, quantity of template DNA, number of contributors to the sample, mixture ratio (i.e., deducible or non-deducible), and level of degradation (moderate, severe, or not degraded). Drop-in rates were estimated separately for low template and high template amplification.

Option	Numerator (Prosecutor's Hypothesis)	Denominator (Defense Hypothesis)
1	Comparison	Unknown
2	Comparison + Known	Known + Unknown
3	Comparison 1 + Comparison 2	2 Unknowns
4	Comparison + Unknown	2 Unknowns
5	Comparison + 2 Unknowns	3 Unknowns
6	Comparison + Known + Unknown	2 Unknowns + Known
7	Comparison + 2 Knowns	Unknown + 2 Knowns

**Table 1A.** Numerator and denominator options available in LR software. "Known" refers to an elimination profile from an individual who is assumed to be a contributor to the evidence sample. "Comparison" refers to the comparison profile of interest (often the suspect). "Unknown" refers to a randomly selected individual from a population of individuals that are unrelated to the Known, Comparison, or to one another.